

FULL PAPER

Computational analysis of new degree-based descriptors of Zig-Zag Benzenoid system

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Chemical graph theory is one of the dominant branches in graph theory. In this paper, we compute the atom bond connectivity, geometric arithmetic, first K-Banhatti, second K-Banhatti, first K-hyper Banhatti, second K-hyper Banhatti, modified first K-Banhatti, modified second K-Banhatti and harmonic K-Banhatti index via M-polynomial of zig-zag Benzenoid system. We also elaborate the result with graphical representation.

KEYWORDS

M-polynomial; Zig-zag Benzenoid; topological indices.

Introduction

Graph theory is one of the most popular and versatile fields of mathematics and has innumerable applications in diverse fields of science like physics, chemistry, operational research, biology and computer science [24]. In chemical graphs, topological indices have great importance. Chemical graph theory is the sub-study of graph theory which reviews and examines the chemical structures of the chemical compounds. A chemical graph basically models the chemical system used to show the interactions like its components, such as atoms, bonds and molecules. It is also called a reaction graph.

In mathematical chemistry, a mathematical tool such as polynomials and numbers predict properties of compounds without utilizing quantum mechanics. These compounds contain information hidden in the molecule. The most common known

invariants of such types are called degree-based topological index.

The first topological index was introduced by Wiener [26]. Topological indices are arithmetic numbers about a graph of the chemical molecules. Every molecule is normally shown by a set of topological indices. Topological variants are derived from hydrogen-suppressed molecular graphs. In theoretical chemistry many topological indices are used to inspect the properties of molecules which are divided into three classes as follows: Distance-dependent, degree-dependent and counted related topological indices. The topological indices also are computed via M-polynomial. Several previous works can be found on this [3-6, 10-20]. Let us define some topological indices.

Atom bond connectivity index

The atom bond connectivity index (ABC) is a molecular structure pattern that has recently

provided a principal application in rationalizing the stability of linear and separate alkanes like as strain energy of cycloalkanes.

$$ABC(G) = \sum_{uv \in E(G)} \sqrt{\frac{d_u + d_v - 2}{d_u \times d_v}}$$

Geometric arithmetic index

In 2009, Damir Vukičević and Boris Furtula used a new index known as geometric arithmetic index [25].

$$GA(G) = \sum_{uv \in E(G)} \frac{2\sqrt{d_u \times d_v}}{d_u + d_v}$$

K-Banhatti and K-hyper Banhatti index

In 2016, V R Kulli proposed some indices [21, 22], named as first K-Banhatti index, second K-Banhatti index, first K-hyper Banhatti index and second K-hyper Banhatti index, defined as

$$B_1(G) = \sum_{uv \in E(G)} (d_u + d_{uv})$$

Second K-Banhatti index

$$B_2(G) = \sum_{uv \in E(G)} (d_u \cdot d_{uv})$$

First K-hyper Banhatti index

$$HB_1(G) = \sum_{uv \in E(G)} (d_u + d_{uv})^2$$

Second K-hyper Banhatti index

$$HB_2(G) = \sum_{uv \in E(G)} (d_u \cdot d_{uv})^2$$

Modified K-Banhatti and Harmonic K-Banhatti index

In 2017, V R Kulli introduced some more indices [23], named as modified first K-Banhatti index, modified second K-Banhatti index and Harmonic K-Banhatti index, and defined as:

Modified first K-Banhatti index

$${}^m B_1(G) = \sum_{uv \in E(G)} \frac{1}{d_u + d_{uv}}$$

Modified second K-Banhatti index

$${}^m B_2(G) = \sum_{uv \in E(G)} \frac{1}{d_u \cdot d_{uv}}$$

Harmonic K-Banhatti index

$$H_b(G) = \sum_{uv \in E(G)} \frac{2}{d_u + d_{uv}}$$

The M-polynomial used [7] is determined as:

$$M(G, x, y) = \sum_{\varphi \leq i \leq j \leq \rho} m_{ij}(G) x^i y^j$$

Where $\varphi = \max\{d_v : v \in V(G)\}$, $\rho = \min\{d_v : v \in V(G)\}$ and $m_{jk}(G)$ is the total number of edges $vu \in E(G)$ where $\{d_v, d_u\} = \{j, k\}$. In last few year many topological indices with the help of M-polynomial have been computed [1,2,4,10-20].

TABLE 1 Degree dependent topological indices via M-polynomial [3]

Topological index	Derivation from M(G;x,y)
Atom-bond connectivity index	$ABC(G) = D_x^{\frac{1}{2}} Q_{-2} J S_x^{\frac{1}{2}} S_y \frac{1}{2} [f(x, y)]_{x=1}$
Geometric arithmetic index	$GA(G) = 2 S_x J D_x^{\frac{1}{2}} D_y^{\frac{1}{2}} [f(x, y)]_{x=1}$
First K-Banhatti index	$B_1(G) = (D_x + D_y + 2 D_x Q_{-2} J) [f(x, y)]_{x=y=1}$
Second K-Banhatti index	$B_2(G) = D_x Q_{-2} J (D_x + D_y) [f(x, y)]_{x=1}$
First K-hyper Banhatti index	$HB_1(G) = (D_x^2 + D_y^2 + 2 D_x^2 Q_{-2} J + 2 D_x Q_{-2} J (D_x + D_y)) [f(x, y)]_{x=y=1}$
Second K-hyper Banhatti index	$HB_2(G) = D_x^2 Q_{-2} J (D_x^2 + D_y^2) [f(x, y)]_{x=1}$
Modified first K-Banhatti index	${}^m B_1(G) = S_x Q_{-2} J (L_x + L_y) [f(x, y)]_{x=1}$

Modified second K-Banhatti index

$${}^m B_2(G) = S_x Q_{-2} J(S_x + S_y)[f(x, y)]_{x=1}$$

Harmonic K-Banhatti index

$$H_b(G) = 2S_x Q_{-2} J(L_x + L_y)[f(x, y)]_{x=1}$$

Where

$$D_x f(x, y) = x \frac{\partial(f(x, y))}{\partial x}, D_y f(x, y) = y \frac{\partial(f(x, y))}{\partial y},$$

$$L_x f(x, y) = f(x^2, y), L_y f(x, y) = f(x, y^2),$$

$$S_x f(x, y) = \int_0^x \frac{f(t, y)}{t} dt, S_y f(x, y) = \int_0^y \frac{f(x, t)}{t} dt,$$

$$Jf(x, y) = f(x, x), Q_a f(x, y) = x^a f(x, y),$$

$$D_x^{\frac{1}{2}} f(x, y) = \sqrt{x \frac{\partial(f(x, y))}{\partial x}} \cdot \sqrt{f(x, y)},$$

$$D_y^{\frac{1}{2}} f(x, y) = \sqrt{y \frac{\partial(f(x, y))}{\partial y}} \cdot \sqrt{f(x, y)},$$

$$S_x^{\frac{1}{2}} f(x, y) = \sqrt{\int_0^x \frac{f(t, y)}{t} dt} \cdot \sqrt{f(x, y)},$$

$$S_y^{\frac{1}{2}} f(x, y) = \sqrt{\int_0^y \frac{f(x, t)}{t} dt} \cdot \sqrt{f(x, y)}.$$

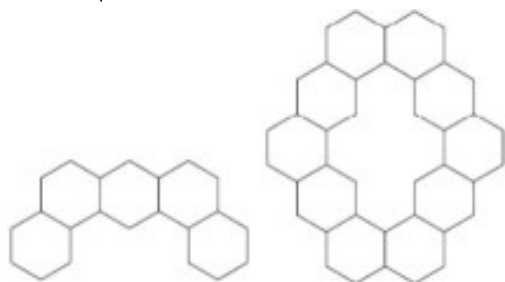


FIGURE 1 Benzenoid system left and non-Benzenoid system right [6]

Zig-zag Benzenoid System

Benzenoid hydrocarbon plays a vital role in our environment and in the food and chemical industry. Benzenoid molecular graphs are systems with deleted hydrogens. Let n represents the number of rows in a graph of zig-zag Benzenoid system Z_n with every row contains two hexagons. The first row contains two hexagons with twelve edges and one edge is common, so we obtain eleven edges in the first row. If we add first and second row, we obtain 24 total edges with three edges that are common, after that we obtain total 21 edges in both rows. Continuing in the same way, we obtain $10n+1$ edges and $8n+2$ vertices.

Consider the zig-zag Benzenoid system Z_n . The Benzenoid system and non-Benzenoid system are shown in Figure 1. The M-polynomial of Z_n which have been compute in [4] is represented as

$$M(Z_n; m, n) = 2(n+2)s^2t^2 + 4ns^2t^3 + (4n-3)s^3t^3.$$

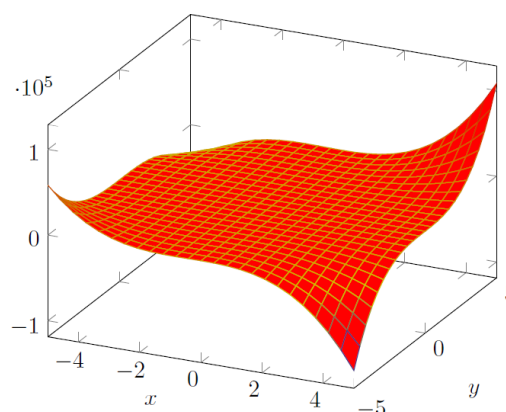


FIGURE 2 3D plot of M-polynomial of zig-zag Benzenoid system for $m=n=2$

Topological indices of Zig-zag Benzenoid system

Theorem 1. Let Z_n be the zig-zag Benzenoid system, then its M-polynomials is

$$M(Z_n; m; n) = (2n+4)s^2t^2 + 4ns^2t^3 + (4n-3)s^3t^3$$

Then

$$[1] ABC[Z_n(m, n)] = \left(\frac{18n + 8\sqrt{2n} + 12 - 6\sqrt{2}}{3\sqrt{2}} \right)$$

$$[2] GA[Z_n(m, n)] = \left(\frac{30n + 8\sqrt{6n} + 5}{5} \right)$$

$$[3] B_1[Z_n(m, n)] = 116n - 10$$

$$[4] B_2[Z_n(m, n)] = 172n - 40$$

$$[5] HB_1[Z_n(m, n)] = 700n - 166$$

$$[6] HB_2[Z_n(m, n)] = 1684n - 736$$

$$[7] {}^m B_1[Z_n(m, n)] = \frac{379n + 120}{105}$$

$$[8] {}^m B_2[Z_n(m, n)] = \frac{50n + 27}{18}$$

$$[9] H_b[Z_n(m, n)] = \frac{758n + 240}{105}$$

Proof. Let

$M(Z_n; m; n) = (2n+4)s^2t^2 + 4ns^2t^3 + (4n-3)s^3t^3$ and by using results from Table 1, we will have:

1. The atom bond connectivity index

$$\begin{aligned} S_1^2 f(s, t) &= \frac{(2n+4)}{\sqrt{2}} s^2 t^2 + \frac{4}{\sqrt{3}} ns^2 t^3 + \frac{(4n-3)}{\sqrt{3}} s^3 t^3 \\ s^3 t^3 S_2^1 S_1^1 f(s, t) &= (n+2)s^2 t^2 + \frac{4}{\sqrt{6}} ns^2 t^3 + \frac{(4n-3)}{3} s^3 t^3 \\ s^3 t^3 JS_2^1 S_1^1 f(s, t) &= (n+2)s^4 + \frac{4}{\sqrt{6}} ns^5 + \frac{(4n-3)}{3} s^6 \\ s^6 Q_2 JS_2^1 S_1^1 f(s, t) &= (n+2)s^2 + \frac{4}{\sqrt{6}} ns^3 + \frac{(4n-3)}{3} s^4 \\ s^4 D_1^1 Q_2 JS_2^1 S_1^1 f(s, t) &= \sqrt{2}(n+2)s^2 + \frac{4}{\sqrt{2}} ns^3 + \frac{(8n-6)}{3} s^4 \\ ABC[Z_n(m, n)] &= D_1^1 Q_2 JS_2^1 S_1^1 [f(s, t)]_{s=t=1} \\ &= \frac{18n + 8\sqrt{2}n + 12 - 6\sqrt{2}}{3\sqrt{2}}. \end{aligned}$$

2. The geometric-arithmetic index

$$\begin{aligned} D_1^1 f(s, t) &= \sqrt{2}(2n+4)s^2 t^2 + \sqrt{3}(4n)s^2 t^3 + \sqrt{3}(4n-3)s^3 t^3 \\ s^3 t^3 D_2^1 D_1^1 f(s, t) &= 2(2n+4)s^2 t^2 + \sqrt{6}(4n)s^2 t^3 + 3(4n-3)s^3 t^3 \\ s^3 t^3 JD_2^1 D_1^1 f(s, t) &= 2(2n+4)s^4 + \sqrt{6}(4n)s^5 + 3(4n-3)s^6 \\ S_3 JD_2^1 D_1^1 f(s, t) &= (n+2)s^4 + \frac{4\sqrt{6}}{5} ns^5 + \frac{(4n-3)}{2} s^6 \\ 2S_3 JD_2^1 D_1^1 f(s, t) &= 2(n+2)s^4 + \frac{8\sqrt{6}}{5} ns^5 + (4n-3)s^6 \\ GA[Z_n(m, n)] &= 2S_3 JD_2^1 D_1^1 [f(s, t)]_{s=t=1} \\ &= \frac{30n + 8\sqrt{6}n + 5}{5}. \end{aligned}$$

3. The first K-Banhatti index

$$\begin{aligned} D_1 f(s, t) &= 2(2n+4)s^2 t^2 + 12ns^2 t^3 + 3(4n-3)s^3 t^3 \\ D_s f(s, t) &= 2(2n+4)s^2 t^2 + 8ns^2 t^3 + 3(4n-3)s^3 t^3 \\ (D_s + D_t) f(s, t) &= 4(2n+4)s^2 t^2 + 20ns^2 t^3 + 6(4n-3)s^3 t^3 \\ (D_s + D_t) f(s, t)_{s=t=1} &= 52n - 2 \\ Jf(s, t) &= (2n+4)s^4 + 4ns^5 + (4n-3)s^6 \\ Q_2 Jf(s, t) &= (2n+4)s^2 + 4ns^3 + (4n-3)s^4 \\ D_s Q_2 Jf(s, t) &= 2(2n+4)s^2 + 12ns^3 + 4(4n-3)s^4 \\ 2D_s Q_2 Jf(s, t) &= 4(2n+4)s^2 + 24ns^3 + 8(4n-3)s^4 \\ 2D_s Q_2 Jf(s, t)_{s=1} &= 64n - 8 \\ B_1[Z_n(m, n)] &= (D_s + D_t + 2D_s Q_2 J)[f(s, t)]_{s=t=1} \\ &= 116n - 10. \end{aligned}$$

4. The second K-Banhatti index

$$\begin{aligned} D_t f(s, t) &= 2(2n+4)s^2 t^2 + 12ns^2 t^3 + 3(4n-3)s^3 t^3 \\ (D_s f(s, t)) &= 2(2n+4)s^2 t^2 + 8ns^2 t^3 + 3(4n-3)s^3 t^3 \\ (D_s + D_t) f(s, t) &= 4(2n+4)s^2 t^2 + 20ns^2 t^3 + 6(4n-3)s^3 t^3 \\ J(D_s + D_t) f(s, t) &= 4(2n+4)s^4 + 20ns^5 + 6(4n-3)s^6 \\ Q_2 J(D_s + D_t) f(s, t) &= 4(2n+4)s^2 + 20ns^3 + 6(4n-3)s^4 \\ D_t Q_2 J(D_s + D_t) f(s, t) &= 8(2n+4)s^2 + 60ns^3 + 24(4n-3)s^4 \\ B_2[Z_n(m, n)] &= D_t Q_2 J(D_s + D_t)[f(s, t)]_{s=1} \\ &= 172n - 40. \end{aligned}$$

5. First K-hyper Bhanhatti index

$$\begin{aligned} D_s^2 f(s, t) &= 4(2n+4)s^2 t^2 + 16ns^2 t^3 + 9(4n-3)s^3 t^3 \\ D_t^2 f(s, t) &= 4(2n+4)s^2 t^2 + 36ns^2 t^3 + 9(4n-3)s^3 t^3 \\ (D_s^2 + D_t^2) f(s, t) &= 8(2n+4)s^2 t^2 + 52ns^2 t^3 \\ &\quad + 18(4n-3)s^3 t^3 \\ (D_s^2 + D_t^2) f(s, t)_{s=t=1} &= 140n - 22 \\ Jf(s, t) &= (2n+4)s^4 + 4ns^5 + (4n-3)s^6 \\ Q_2 Jf(s, t) &= (2n+4)s^2 + 4ns^3 + (4n-3)s^4 \\ D_s^2 Q_2 Jf(s, t) &= 4(2n+4)s^2 + 36ns^3 + 16(4n-3)s^4 \\ 2D_s^2 Q_2 Jf(s, t) &= 8(2n+4)s^2 + 72ns^3 + 32(4n-3)s^4 \\ 2D_s^2 Q_2 J[f(s, t)]_{s=1} &= 216n - 64 \\ D_t f(s, t) &= 2(2n+4)s^2 t^2 + 12ns^2 t^3 + 3(4n-3)s^3 t^3 \\ (D_s f(s, t)) &= 2(2n+4)s^2 t^2 + 8ns^2 t^3 + 3(4n-3)s^3 t^3 \\ (D_s + D_t) f(s, t) &= 4(2n+4)s^2 t^2 + 20ns^2 t^3 + 6(4n-3)s^3 t^3 \\ J(D_s + D_t) f(s, t) &= 4(2n+4)s^4 + 20ns^5 + 6(4n-3)s^6 \\ Q_2 J(D_s + D_t) f(s, t) &= 4(2n+4)s^2 + 20ns^3 + 6(4n-3)s^4 \\ D_s Q_2 J(D_s + D_t) f(s, t) &= 8(2n+4)s^2 + 60ns^3 + 24(4n-3)s^4 \\ 2D_s Q_2 J(D_s + D_t) f(s, t) &= 16(2n+4)s^2 + 120ns^3 + 48(4n-3)s^4 \\ 2D_s Q_2 J(D_s + D_t)[f(s, t)]_{s=1} &= 344n - 80 \\ HB_1[Z_n(m, n)] &= (D_s^2 + D_t^2 + 2D_s^2 Q_2 J \\ &\quad + 2D_s Q_2 J(D_s + D_t))[f(s, t)]_{s=t=1} = 700n - 166. \end{aligned}$$

6. Second K-hyper Bhanhatti index

$$\begin{aligned} D_s^2 f(s, t) &= 4(2n+4)s^2 t^2 + 16ns^2 t^3 + 9(4n-3)s^3 t^3 \\ D_t^2 f(s, t) &= 4(2n+4)s^2 t^2 + 36ns^2 t^3 + 9(4n-3)s^3 t^3 \\ (D_s^2 + D_t^2) f(s, t) &= 8(2n+4)s^2 t^2 + 52ns^2 t^3 + 18(4n-3)s^3 t^3 \\ J(D_s^2 + D_t^2) f(s, t) &= 8(2n+4)s^4 + 52ns^5 + 18(4n-3)s^6 \\ Q_2 J(D_s^2 + D_t^2) f(s, t) &= 8(2n+4)s^2 + 52ns^3 + 18(4n-3)s^4 \\ D_s^2 Q_2 J(D_s^2 + D_t^2) f(s, t) &= 32(2n+4)s^2 \\ &\quad + 468ns^3 + 288(4n-3)s^4 \\ HB_2[Z_n(m, n)] &= D_s^2 Q_2 J(D_s^2 + D_t^2)[f(s, t)]_{s=1} \\ &= 1684n - 736. \end{aligned}$$

7. Modified first K-Banhatti index

$$L_s f(s,t) = (2n+4)s^4 t^2 + 4ns^4 t^3 + (4n-3)s^6 t^3$$

$$L_t f(s,t) = (2n+4)s^2 t^4 + 4ns^2 t^6 + (4n-3)s^3 t^6$$

$$J(L_s + L_t) f(s,t) = 2(2n+4)s^6 + 4n(s^7 + s^8) + 2(4n-3)s^9$$

$$Q_{-2} J(L_s + L_t) f(s,t) = 2(2n+4)s^4 + 4n(s^5 + s^6) + 2(4n-3)s^7$$

$$S_s Q_{-2} J(L_s + L_t) f(s,t) = \frac{(2n+4)}{2} s^4 + 4n\left(\frac{1}{5} s^5 + \frac{1}{6} s^6\right) + \frac{(8n-6)}{7} s^7$$

$${}^m B_1[Z_n(m,n)] = S_s Q_{-2} J(L_s + L_t) [f(s,t)]_{s=1}$$

$$= \frac{379n + 120}{105}$$

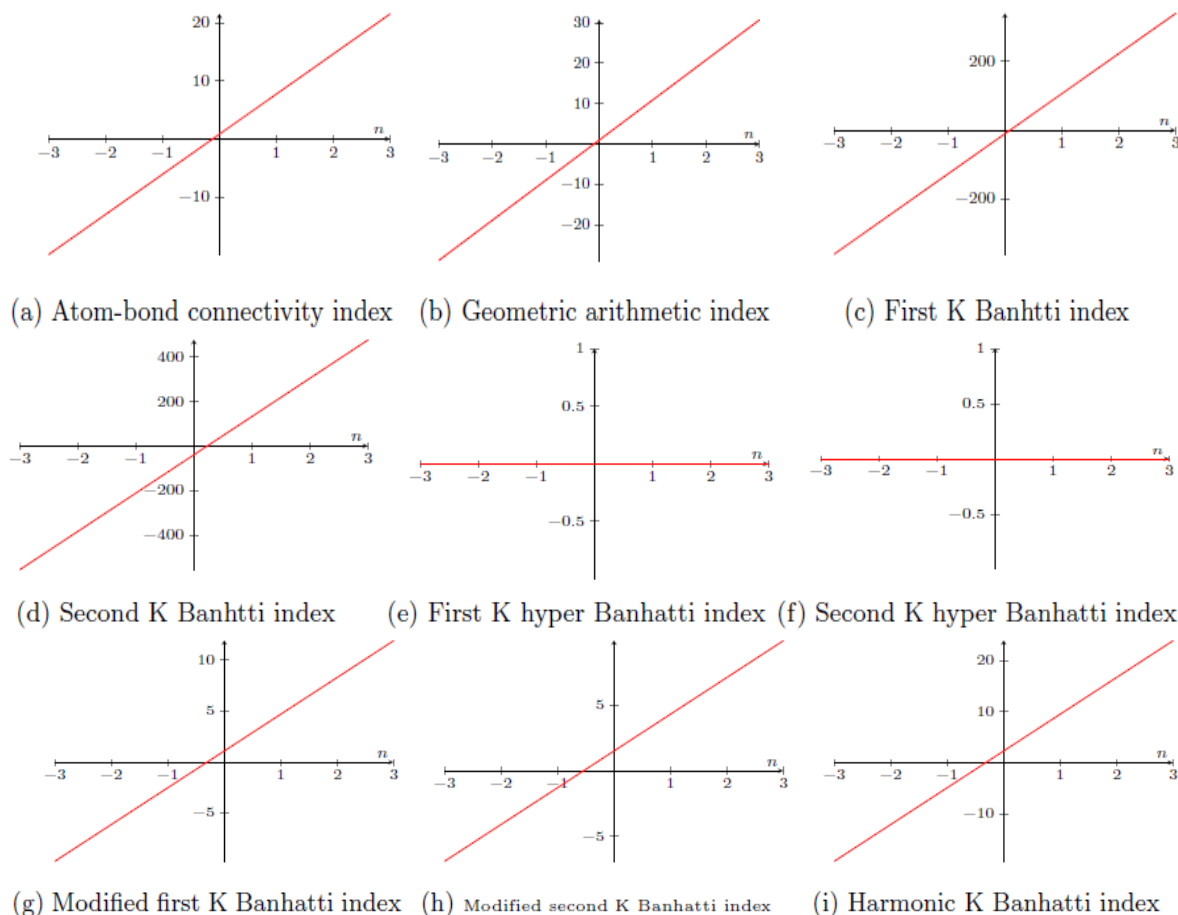


FIGURE 3 The plot of topological indices of Zig-zag Benzenoid graph Z_n

8. Modified second K-Banhatti index

$$S_s f(s,t) = (n+2)s^2 t^2 + 2ns^2 t^3 + \frac{(4n-3)}{3} s^3 t^3$$

$$S_t f(s,t) = (n+2)s^2 t^2 + \frac{4n}{3} s^2 t^3 + \frac{(4n-3)}{3} s^3 t^3$$

$$(S_s + S_t) f(s,t) = 2(n+2)s^2 t^2 + \frac{10}{3} ns^2 t^3 + \frac{(8n-6)}{3} s^3 t^3$$

$$J(S_s + S_t) f(s,t) = 2(n+2)s^4 + \frac{10}{3} ns^5 + \frac{(8n-6)}{3} s^6$$

$$Q_{-2} J(S_s + S_t) f(s,t) = 2(n+2)s^2 + \frac{10}{3} ns^3 + \frac{(8n-6)}{3} s^4$$

$$S_s Q_{-2} J(S_s + S_t) f(s,t) = (n+2)s^2 + \frac{10}{9} ns^3 + \frac{(8n-6)}{12} s^4$$

$${}^m B_2[Z_n(m,n)] = S_s Q_{-2} J(S_s + S_t) [f(s,t)]_{s=1} = \frac{50n + 27}{18}$$

9. Harmonic K-Banhatti index

$$L_s f(s,t) = (2n+4)s^4 t^2 + 4ns^4 t^3 + (4n-3)s^6 t^3$$

$$L_t f(s,t) = (2n+4)s^2 t^4 + 4ns^2 t^6 + (4n-3)s^3 t^6$$

$$J(L_s + L_t) f(s,t) = 2(2n+4)s^6 + 4n(s^7 + s^8) + 2(4n-3)s^9$$

$$Q_{-2} J(L_s + L_t) f(s,t) = 2(2n+4)s^4 + 4n(s^5 + s^6) + 2(4n-3)s^7$$

$$S_s Q_{-2} J(L_s + L_t) f(s,t) = \frac{(2n+4)}{2} s^4 + 4n\left(\frac{1}{5} s^5 + \frac{1}{6} s^6\right) + \frac{(8n-6)}{7} s^7$$

$$2S_s Q_{-2} J(L_s + L_t) f(s,t) = (2n+4)s^4 + 8n\left(\frac{1}{5} s^5 + \frac{1}{6} s^6\right) + \frac{(16n-12)}{7} s^7$$

$$H_b[Z_n(m, n)] = 2S_s Q_{-2} J(L_s + L_t) [f(s, t)]_{s=1} \\ = \frac{758n + 240}{105}.$$

Conclusion

In this paper, we computed the degree-based topological indices via M-polynomial of Benzenoid system. This polynomial was improved to calculate the topological indices values of the molecular structure. We plotted graphs of M-polynomial against the number of hexagon n in every diagram. These indices play a principal role in finding the properties of the chemical compounds.

Graphical analyses

The 3-dimensional and 2-dimensional plots of M-polynomial of Zig-zag Benzenoid graph Z_n are shown in figures 2 and 3, respectively.

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